$\qquad$

LESSON
11.4 Study Guide
For use with the lesson "Find Probabilities of Disjoint and Overlapping Events"

GOAL Find probabilities of compound events.

## Vocabulary

The union or intersection of two events is called a compound event.
Two events are overlapping if they have one or more outcomes in common.

Two events are disjoint, or mutually exclusive, if they have no outcomes in common.

## EXAMPLE 1 Find probability of disjoint events

A card is randomly selected from a standard deck of 52 cards. What is the probability that it is a 5 or an ace?

Let event $A$ be selecting a 5 and event $B$ be selecting an ace. $A$ has 4 outcomes and $B$ has 4 outcomes. Because $A$ and $B$ are disjoint, the probability is:
$P(A$ or $B)=P(A)+P(B)=\frac{4}{52}+\frac{4}{52}=\frac{8}{52}=\frac{2}{13} \approx 0.154$

## EXAMPLE 2 Find probability of overlapping events

A card is randomly selected from a standard deck of $\mathbf{5 2}$ cards. What is the probability that it is a club or a 3?
Let event $A$ be selecting a club and event $B$ be selecting a 3. $A$ has 13 outcomes and $B$ has 4 outcomes. Of these, 1 outcome is common to $A$ and $B$. The probability of selecting a club or a 3 is:
$P(A$ or $B)=P(A)+P(B)-P(A$ and $B)=\frac{13}{52}+\frac{4}{52}-\frac{1}{52}=\frac{16}{52}=\frac{4}{13} \approx 0.308$

## EXAMPLE 3 Use a formula to find P(A and B)

Given $\boldsymbol{P}(\mathbf{A})=\mathbf{0 . 3}, \boldsymbol{P}(\boldsymbol{B})=\mathbf{0 . 7 2}$, and $\boldsymbol{P}(\boldsymbol{A}$ or $\boldsymbol{B})=\mathbf{0 . 6}$, find $\boldsymbol{P}(\mathbf{A}$ and $\boldsymbol{B})$.

$$
\begin{aligned}
P(A \text { or } B) & =P(A)+P(B)-P(A \text { and } B) & & \text { Write general formula. } \\
0.6 & =0.3+0.72-P(A \text { and } B) & & \text { Substitute known probabilities. } \\
P(A \text { and } B) & =0.42 & & \text { Solve for } P(A \text { and } B) .
\end{aligned}
$$

## Exercises for Examples 1, 2, and 3

A card is randomly selected from a standard deck of 52 cards. Find the probability of the given event.

1. Selecting a queen or a 4 2. Selecting a spade or a 5
2. Find $P(A$ and $B)$ when $P(A)=0.25, P(B)=0.40$, and $P(A$ or $B)=0.55$.
$\qquad$

## EXAMPLE 4 Find probabilities of complements

When two six-sided dice are rolled, there are 36 possible outcomes. Find the probability of the given event.
a. The sum is less than or equal to 3 .
b. The sum is greater than 3 .

## Solution

a. The outcomes for which the sum is less than or equal to 3 are
$(1,1),(2,1)$, and $(1,2)$.
$P($ sum $\leq 3)=\frac{3}{36}=\frac{1}{12} \approx 0.083$
b. $\quad P(\operatorname{sum}>3)=1-P(\operatorname{sum} \leq 3)$

$$
\begin{aligned}
& =1-\frac{1}{12} \\
& =\frac{11}{12} \\
& \approx 0.917
\end{aligned}
$$

## EXAMPLE 5 Use a complement in real life

Annual Salary A university conducted a national research study of recipients of PhD degrees. From the research data, the university determined that the probability that these recipients had annual salaries in excess of $\$ 95,000$ was 0.834 . What is the probability that a recipient from the study had an annual salary of $\$ 95,000$ or less?

## Solution

The probability that a recipient had an annual salary of $\$ 95,000$ or less is the complement of the event that a recipient had an annual salary in excess of $\$ 95,000$.

$$
\begin{aligned}
P(\text { salary } \leq \$ 95,000) & =1-P(\text { salary }>\$ 95,000) \\
& =1-0.834 \\
& =0.166
\end{aligned}
$$

## Exercises for Examples 4 and 5

## Find $\boldsymbol{P}(\overline{\boldsymbol{A}})$.

4. $P(A)=0.63$
5. $P(A)=\frac{1}{8}$
6. $P(A)=0.45$
7. $P(A)=0.09$
8. In Example 5 if the probability that the recipients of PhD degrees had annual salaries in excess of $\$ 95,000$ was 0.668 , what is the probability that a recipient from the study had an annual salary of $\$ 95,000$ or less?
