

LESSON
2.7**Study Guide**

For use with the lesson "Solve Proportions Using Cross Products"

GOAL Solve proportions using cross products.**Vocabulary**

In a proportion, a **cross product** is the product of the numerator of one ratio and the denominator of the other ratio.

Cross Products Property

The cross products of a proportion are equal.

If $\frac{a}{b} = \frac{c}{d}$ where $b \neq 0$ and $d \neq 0$, then $ad = bc$.

A **scale drawing** is a two-dimensional drawing of an object in which the dimensions of the drawing are in proportion to the dimensions of the object.

A **scale model** is a three-dimensional model of an object in which the dimensions of the model are in proportion to the dimensions of the object.

The **scale** of a scale drawing or scale model relates the drawing's or model's dimensions and the actual dimensions.

EXAMPLE 1 Solve a proportion using the cross products property

Solve $\frac{20}{35} = \frac{8}{x}$.

Solution

$$\frac{20}{35} = \frac{8}{x} \quad \text{Write original proportion.}$$

$$20 \cdot x = 8 \cdot 35 \quad \text{Cross products property}$$

$$20x = 280 \quad \text{Simplify.}$$

$$x = 14 \quad \text{Divide each side by 20.}$$

The solution is 14. Check your solution by substituting 14 for x in the original proportion.

Exercises for Example 1

Solve the proportion. Check your solution.

1. $\frac{15}{x} = \frac{126}{210}$

2. $\frac{y+8}{21} = \frac{y}{9}$

3. $\frac{28}{z} = \frac{24}{z-5}$

LESSON
2.7**Study Guide** *continued**For use with the lesson "Solve Proportions Using Cross Products"***EXAMPLE 2** **Write and solve a proportion**

A bag of large breed dog food recommends feeding a dog 3 cups of food a day for every 40 pounds of body weight. A dog weights 98 pounds. How much food should the dog be eating each day?

Solution

STEP 1 Write a proportion involving two ratios that compare the amount of dog food to the weight of the dog.

$$\frac{3}{40} = \frac{x}{98} \quad \begin{array}{l} \leftarrow \text{cups of food} \\ \leftarrow \text{weight of dog} \end{array}$$

STEP 2 Solve the proportion.

$$\frac{3}{40} = \frac{x}{98} \quad \text{Write proportion.}$$

$$3 \cdot 98 = 40 \cdot x \quad \text{Cross products property}$$

$$294 = 40x \quad \text{Simplify.}$$

$$7.35 = x \quad \text{Divide each side by 40.}$$

A 98-pound dog should eat 7.35 cups of food each day.

EXAMPLE 3 **Use the scale on a blueprint**

A blueprint of an office building has a scale of 2 inches:15 feet. A completed scale model of the building is about 14.5 inches tall. Estimate the actual height of the office building.

Solution

STEP 1 Write a proportion to find the height x of the office building.

$$\frac{2}{15} = \frac{14.5}{x} \quad \begin{array}{l} \leftarrow \text{inches} \\ \leftarrow \text{feet} \end{array}$$

STEP 2 Solve the proportion.

$$\frac{2}{15} = \frac{14.5}{x} \quad \text{Write proportion.}$$

$$2 \cdot x = 14.5 \cdot 15 \quad \text{Cross products property}$$

$$2x = 217.5 \quad \text{Simplify.}$$

$$x = 108.75 \quad \text{Divide each side by 2.}$$

The height of the office building is about 108.75 feet.

Exercises for Examples 2 and 3

4. A car travels 135 miles on 4 gallons of gasoline. How many gallons of gasoline will be used to travel 540 miles?

A blueprint has a scale of 3 cm : 5 m. Use the given measurement to find the actual distance.

5. 4.5 cm

6. 8.1 cm

7. 0.6 cm