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LESSON
2.8

GOAL Write equations in function form and rewrite formulas.

## Vocabulary

An equation in $x$ and $y$ is written in function form when the dependent variable $y$ is isolated on one side of the equation.

A literal equation is an equation that contains two or more variables.

## EXAMPLE 1 Rewrite an equation in function form

## Write $9 x-4 y=8$ in function form.

## Solution

To write an equation in function form, solve the equation for $y$.

$$
\begin{aligned}
9 x-4 y & =8 & & \text { Write original equation. } \\
-4 y & =8-9 x & & \text { Subtract } 9 x \text { from each side. } \\
y & =-2+\frac{9}{4} x & & \text { Divide each side by }-4 .
\end{aligned}
$$

The equation $y=-2+\frac{9}{4} x$ is written in function form.

## EXAMPLE2 Solve a literal equation

The formula for the volume of a rectangular prism is $\boldsymbol{V}=\ell \boldsymbol{w h}$. Solve the formula for $\ell$.

## Solution

$V=\ell w h \quad$ Write original equation.
$\frac{V}{w h}=\frac{\ell w h}{w h} \quad$ Assume $w \neq 0$ and $h \neq 0$. Divide each side by $w h$.
$\frac{V}{w h}=\ell \quad$ Simplify.
The rewritten equation is $\frac{V}{w h}=\ell$.

## Exercises for Examples 1 and 2

Write the equation in function form.

1. $7 x+y=12$
2. $3 y-9 x=21$
3. $5 y-2 x=15$

Solve the literal equation.
4. $I=\operatorname{Prt}$ for $P$
5. $A=\frac{1}{2}\left(b_{1}+b_{2}\right) h$ for $b_{2}$
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## LESSON

## EXAMPLE 3 Solve and use a geometric formula

The area $A$ of a triangle is given by the formula $A=\frac{1}{2} b h$ where $b$ is the base and $h$ is the height.

a. Solve the formula for the base $b$.
b. Use the rewritten formula to find the base of the triangle shown, which has an area of 106.8 square inches.

## Solution

a. Solve the formula for $b$.

$$
\begin{aligned}
A & =\frac{1}{2} b h & & \text { Write original formula. } \\
2 A & =b h & & \text { Multiply each side by } 2 . \\
\frac{2 A}{h} & =b & & \text { Divide each side by } h .
\end{aligned}
$$

b. Substitute 106.8 for $A$ and 12 for $h$ in the rewritten formula.

$$
\begin{array}{ll}
b=\frac{2 A}{h} & \text { Write rewritten formula. } \\
b=\frac{2(106.8)}{12} & \\
\text { Substitute } 106.8 \text { for } A \text { and } 12 \text { for } h . \\
b=17.8 & \\
\text { Simplify. }
\end{array}
$$

The base of the triangle is 17.8 inches.

## Exercises for Example 3

The surface area $S$ of a sphere is given by the formula $S=4 \pi r^{2}$ where $r$ is the radius of the sphere.
6. Solve the formula for $r$.
7. Use the rewritten formula from Exercise 6 to find $r$ when $S=314$ square meters. Use 3.14 for $\pi$.

