Study Guide

For use with the lesson "Rewrite Equations and Formulas"

GOAL

Write equations in function form and rewrite formulas.

Vocabulary

An equation in x and y is written in **function form** when the dependent variable y is isolated on one side of the equation.

A literal equation is an equation that contains two or more variables.

EXAMPLE 1

Rewrite an equation in function form

Write 9x - 4y = 8 in function form.

Solution

To write an equation in function form, solve the equation for y.

$$9x - 4y = 8$$

Write original equation.

$$-4v = 8 - 9v$$

-4v = 8 - 9x Subtract 9x from each side.

$$y = -2 + \frac{9}{4}x$$

 $y = -2 + \frac{9}{4}x$ Divide each side by -4.

The equation $y = -2 + \frac{9}{4}x$ is written in function form.

EXAMPLE 2

Solve a literal equation

The formula for the volume of a rectangular prism is $V = \ell wh$. Solve the formula for ℓ .

Solution

$$V = \ell w h$$

Write original equation.

$$\frac{V}{wh} = \frac{\ell wh}{wh}$$

Assume $w \neq 0$ and $h \neq 0$. Divide each side by wh.

$$\frac{V}{wh} = \ell$$

Simplify.

The rewritten equation is $\frac{V}{wh} = \ell$.

Exercises for Examples 1 and 2

Write the equation in function form.

1.
$$7x + y = 12$$

2.
$$3y - 9x = 21$$

3.
$$5y - 2x = 15$$

Solve the literal equation.

4.
$$I = Prt \text{ for } P$$

5.
$$A = \frac{1}{2}(b_1 + b_2)h$$
 for b_2

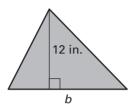
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EXAMPLE 3

Solve and use a geometric formula

The area A of a triangle is given by the formula $A = \frac{1}{2}bh$ where b is the base and h is the height.



- **a.** Solve the formula for the base b.
- **b.** Use the rewritten formula to find the base of the triangle shown, which has an area of 106.8 square inches.

Solution

a. Solve the formula for *b*.

$$A = \frac{1}{2}bh$$
 Write original formula.

$$2A = bh$$
 Multiply each side by 2.

$$\frac{2A}{h} = b$$
 Divide each side by h .

b. Substitute 106.8 for A and 12 for h in the rewritten formula.

$$b = \frac{2A}{h}$$
 Write rewritten formula.

$$b = \frac{2(106.8)}{12}$$
 Substitute 106.8 for *A* and 12 for *h*.

$$b = 17.8$$
 Simplify.

The base of the triangle is 17.8 inches.

Exercises for Example 3

The surface area S of a sphere is given by the formula $S = 4\pi r^2$ where r is the radius of the sphere.

- **6.** Solve the formula for r.
- **7.** Use the rewritten formula from Exercise 6 to find r when S = 314 square meters. Use 3.14 for π .