Study Guide

For use with the lesson "Graph Using Slope-Intercept Form"

GOAL

Graph linear equations using slope-intercept form.

Vocabulary

A linear equation of the form y = mx + b is written in **slope-intercept form**, where m is the slope and b is the y-intercept of the equation's graph.

Two lines in the same plane are **parallel** if they do not intersect.

EXAMPLE 1

Identify the slope and y-intercept

Identify the slope and y-intercept of the line with the given equation.

a.
$$y = \frac{1}{4}x - 2$$

b.
$$-2x + 3y = 9$$

Solution

- **a.** The equation is in the form y = mx + b. So, the slope of the line is $\frac{1}{4}$, and the y-intercept is -2.
- **b.** Rewrite the equation in slope-intercept form by solving for y.

$$-2x + 3y = 9$$

Write original equation.

$$3y = 2x + 9$$

Add 2x to each side.

$$y = \frac{2}{3}x + 3$$

 $y = \frac{2}{3}x + 3$ Divide each side by 3.

The line has a slope of $\frac{2}{3}$ and a y-intercept of 3.

Exercises for Example 1

Identify the slope and y-intercept of the line with the given equation.

1.
$$y = -3x + 7$$

2.
$$15x - 5y = 10$$
 3. $-x - 6y = 18$

3.
$$-x - 6y = 18$$

LESSON 3.5

Study Guide continued

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EXAMPLE 2 Graph an equation using slope-intercept form

Graph the equation 4x + y = 3.

Solution

STEP 1 Rewrite the equation in slope-intercept form.

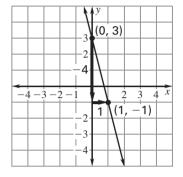
$$v = -4x + 3$$

STEP 2 Identify the slope and the *y*-intercept.

$$m = -4$$
 and $b = 3$

STEP 3 Plot the point that corresponds to the *y*-intercept, (0, 3).

STEP 4 Use the slope to locate a second point on the line. Draw a line through the two points.



Exercises for Example 2

Graph the equation.

4.
$$y = \frac{3}{4}x - 1$$

5.
$$y = -x$$

EXAMPLE 3 Identify

Identify parallel lines

Determine which of the lines are parallel: line a through (-3, 1) and (-6, 7); line b through (-7, -5) and (1, 11); line c through (2, 5) and (4, 9).

Solution

Find the slope of each line.

Line *a*:
$$m = \frac{7-1}{-6-(-3)} = \frac{6}{-3} = -2$$

Line *b*:
$$m = \frac{11 - (-5)}{1 - (-7)} = \frac{16}{8} = 2$$

Line
$$c$$
: $m = \frac{9-5}{4-2} = \frac{4}{2} = 2$

Line b and line c have the same slope, so they are parallel.

Exercise for Example 3

6. Determine which of the lines are parallel: line a through (5, 3) and (8, 5); line b through (-2, 9) and (1, 11); line c through (12, 8) and (8, 2).