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GOAL Graph linear equations using slope-intercept form.

## Vocabulary

A linear equation of the form $y=m x+b$ is written in slope-intercept form, where $m$ is the slope and $b$ is the $y$-intercept of the equation's graph.

Two lines in the same plane are parallel if they do not intersect.

## EXAMPLE 1 Identify the slope and $\boldsymbol{y}$-intercept

Identify the slope and $y$-intercept of the line with the given equation.
a. $y=\frac{1}{4} x-2$
b. $-2 x+3 y=9$

## Solution

a. The equation is in the form $y=m x+b$. So, the slope of the line
is $\frac{1}{4}$, and the $y$-intercept is -2 .
b. Rewrite the equation in slope-intercept form by solving for $y$.

$$
\begin{aligned}
-2 x+3 y & =9 & & \text { Write original equation. } \\
3 y & =2 x+9 & & \text { Add } 2 x \text { to each side. } \\
y & =\frac{2}{3} x+3 & & \text { Divide each side by } 3 .
\end{aligned}
$$

The line has a slope of $\frac{2}{3}$ and a $y$-intercept of 3 .

## Exercises for Example 1

Identify the slope and $\boldsymbol{y}$-intercept of the line with the given equation.

1. $y=-3 x+7$
2. $15 x-5 y=10$
3. $-x-6 y=18$
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$\qquad$ 3.5 Study Guide continued

## EXAMPLE2 Graph an equation using slope-intercept form

Graph the equation $4 x+y=3$.

## Solution

STEP 1 Rewrite the equation in slope-intercept form.

$$
y=-4 x+3
$$

STEP 2 Identify the slope and the $y$-intercept.
$m=-4$ and $b=3$
STEP 3 Plot the point that corresponds to the $y$-intercept, $(0,3)$.

STEP 4 Use the slope to locate a second point on
 the line. Draw a line through the two points.

## Exercises for Example 2

Graph the equation.
4. $y=\frac{3}{4} x-1$
5. $y=-x$

## EXAMPLE 3 Identify parallel lines

Determine which of the lines are parallel: line a through $(-3,1)$ and $(-6,7)$; line $b$ through $(-7,-5)$ and $(1,11)$; line $c$ through $(2,5)$ and $(4,9)$.

## Solution

Find the slope of each line.
Line $\boldsymbol{a}: m=\frac{7-1}{-6-(-3)}=\frac{6}{-3}=-2$
Line $\boldsymbol{b}$ : $m=\frac{11-(-5)}{1-(-7)}=\frac{16}{8}=2$
Line $c: m=\frac{9-5}{4-2}=\frac{4}{2}=2$
Line $b$ and line $c$ have the same slope, so they are parallel.

## Exercise for Example 3

6. Determine which of the lines are parallel: line $a$ through $(5,3)$ and $(8,5)$; line $b$ through $(-2,9)$ and $(1,11)$; line $c$ through $(12,8)$ and $(8,2)$.
