(1, 3)

 $\frac{1}{3}$ \hat{x}

GOAL

Write equations in standard form.

EXAMPLE 1

Write equivalent equations in standard form

Write two equations in standard form that are equivalent to 3x - 9y = 12.

Solution

To write one equivalent equation, multiply each side by $\frac{1}{3}$.

$$x - 3y = 4$$

To write another equivalent equation, multiply each side by 2.

-5 - 4 - 3 - 2

(-2, -3)

$$6x - 18y = 24$$

EXAMPLE 2

Write an equation from a graph

Write an equation in standard form of the line shown.

Solution

STEP 1 Calculate the slope.

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{3+3}{1+2} = \frac{6}{3} = 2$$

STEP 2 Write an equation in point-slope form.

Use
$$(1, 3)$$
.

$$y - y_1 = m(x - x_1)$$

Write point-slope form.

$$y - 3 = 2(x - 1)$$

Substitute 2 for m, 1 for x, and 3 for y.

STEP 3 Rewrite the equation in standard form.

$$y - 3 = 2x - 2$$

Distributive property

$$-2x + v = 1$$

Collect variable terms on one side, constants on the other.

Exercises for Examples 1 and 2

1. Write two equations in standard form that are equivalent to 6x + 2y = 8.

Write an equation in standard form of the line that passes through the given points.

3.
$$(-2,3), (-4,-5)$$

For use with the lesson "Write Linear Equations in Standard Form"

EXAMPLE3 Write an equation of a line

Write equations of the horizontal and vertical lines that pass through the point (-2, 8).

Solution

The horizontal line has all the same y-coordinates. The y-coordinate of the given point is 8. So, an equation of the horizontal line is y = 8.

The vertical line has all the same *x*-coordinates. The *x*-coordinate of the given point is -2. So, an equation of the vertical line is x = -2.

Exercises for Example 3

Write equations of the horizontal and vertical lines that pass through the given point.

5.
$$(-1, 5)$$

EXAMPLE 4 Complete an equation in standard form

The graph of 5x + By = 6 is a line that passes through the point (2, 1). Find the missing coefficient and write the completed equation.

Solution

STEP 1 Find the value of B. Substitute the coordinates of the given point for x and y in the equation. Solve for B.

$$5x + By = 6$$
 Write equation.

$$5(2) + B(1) = 6$$
 Substitute 2 for x and 1 for y.

$$B = -4$$
 Simplify.

STEP 2 Complete the equation.

$$5x - 4y = 6$$
 Substitute -4 for B .

The completed equation is 5x - 4y = 6.

Exercises for Example 4

Find the missing coefficient in the equation of the line that passes through the given point. Write the completed equation.

6.
$$Ax + 5y = 7$$
, (4, 3)

7.
$$4x + By = 6, (3, -2)$$