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LESSON
6.5

## Challenge Practice

For use with the lesson "Solve Special Types of Linear Systems"

## In Exercises 1-3, use the linear system.

$a x+\frac{1}{4} y=7$
$\frac{1}{3} x+\frac{1}{6} y=3$

1. For what values of $a$ does the system have no solution?
2. For what values of $a$ does the system have infinitely many solutions?
3. For what values of $a$ does the system have exactly one solution?

## In Exercises 4 and 5, suppose $a, b$, and $c$ are non-zero constants. Use the linear system.

$$
\begin{aligned}
& a x+b y=3 \\
& c a x+c b y=12
\end{aligned}
$$

4. Does the number of solutions depend on the values of $a, b$, and $c$ ?
5. Describe the number of solutions in each possible case.

In Exercises 6-9, suppose $a_{1}, a_{2}, b_{1}, b_{2}, c_{1}$, and $c_{2}$ are non-zero constants.
Use the linear system.

```
a
a}\mp@subsup{a}{2}{}x+\mp@subsup{b}{2}{}y=\mp@subsup{c}{2}{
```

6. Solve for $x$ and $y$ in terms of $a_{1}, a_{2}, b_{1}, b_{2}, c_{1}$, and $c_{2}$.
7. State the relationship between the values of $a_{1}, a_{2}, b_{1}, b_{2}, c_{1}$, and $c_{2}$ that will guarantee there is exactly one solution.
8. State the relationship between the values of $a_{1}, a_{2}, b_{1}, b_{2}, c_{1}$, and $c_{2}$ that will guarantee there is no solution.
9. State the relationship between the values of $a_{1}, a_{2}, b_{1}, b_{2}, c_{1}$, and $c_{2}$ that will guarantee there are infinitely many solutions.

## Lesson 6.5 Solve S pecial Types of Linear Systems, continued

## Study Guide

1. infinitely many solutions
2. no solution
3. infinitely many solutions
4. one solution
5. one solution

## Real-Life Application

1. 



Yes, there is a possibility because the two lines intersect.
2. The two equations represent the same line. If the cubs are walking towards you, then yes, you will see them. If the cubs are walking away from you, then no, you will not see them. 3. No, you will not cross the stream. The two lines are parallel.

## Challenge Practice

1. $a=\frac{1}{2}$
2. No value of $a$ gives infinitely many solutions. 3. $a \neq \frac{1}{2}$ 4. The number of solutions depends only on the value of $c$. 5. When $c=4$ there are an infinite number of solutions. When $c \neq 4$ there are no solutions.
3. $x=\frac{c_{1} b_{2}-c_{2} b_{1}}{a_{1} b_{2}-a_{2} b_{1}} ; y=\frac{a_{1} c_{2}-a_{2} c_{1}}{a_{1} b_{2}-a_{2} b_{1}}$
4. $a_{1} b_{2} \neq a_{2} b_{1}$
5. $a_{1} b_{2}=a_{2} b_{1}$ and $c_{2} \neq \frac{b_{2}}{b_{1}} c_{1}$
6. $a_{1} b_{2}=a_{2} b_{1}$ and $c_{2}=\frac{b_{2}}{b_{1}} c_{1}$

## Lesson 6.6 Solve Systems of Linear Inequalities

## Teaching Guide

1. 


4. The shaded region is the intersection of the regions that are the solutions of the two inequalities.

## Spreadsheet Activity

1. not a solution; not a solution; solution; not a solution 2. solution; not a solution; not a solution; solution

## Practice Level A

1. yes
2. no
3. yes
4. no
5. yes
6. yes
7. D
8. B
9. A
10. C
11. F 12. E
12. 


15.

17.

14.

16.

18.

19. a. $x+y \leq 10$ and $15 x+18 y \leq 90$
b.

20. a. 6 h

c. Answers will vary.

