Investigating Algebra Activity: Quotients and Powers

For use before the lesson "Apply Exponent Properties Involving Quotients"

Materials: paper and pencil

OUESTION How can you find the quotient of a power and the power of a quotient?

EXPLORE 1 Find the quotient of a power

STEP 1 Copy and complete the table below.

Expression	Expanded form	Simplified expanded form	Number of factors	Simplified expression
$\frac{5^7}{5^3}$	<u>5 • 5 • 5 • 5 • 5 • 5</u> <u>5 • 5 • 5</u>	5 • 5 • 5 • 5	4	5 ⁴
$\frac{x^6}{x^2}$				

STEP 2 Analyze the results

Find a pattern between the exponents of the expression in the first column and the exponent of the expression in the last column.

EXPLORE 2 Find the power of a quotient

STEP 1 Copy and complete the table below.

Expression	Expanded form	Expression as repeated multiplication	Simplified expression
$\left(\frac{2x^3}{3}\right)^3$	$\left(\frac{2x^3}{3}\right)\left(\frac{2x^3}{3}\right)\left(\frac{2x^3}{3}\right)$	$\frac{2 \cdot 2 \cdot 2 \cdot x^3 \cdot x^3 \cdot x^3}{3 \cdot 3 \cdot 3}$	$\frac{2^3x^9}{3^3}$
$\left(\frac{5x^3y}{4}\right)^2$			

STEP 2 Analyze the results

Find a pattern between the exponents of the expression in the first column and the exponents of the expression in the last column.

DRAW CONCLUSIONS

Use your observations to complete these statements.

- **1.** If a is a nonzero real number and m and n are positive integers with m > n, then $\frac{a^m}{a^n} = \underline{}$?.
- **2.** If a and b are real numbers with $b \neq 0$ and m a positive integer, then $\left(\frac{a}{b}\right)^m = \underline{}.$