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CHAPTER REVIEW

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- Multi-Language Glossary
- Vocabulary practice

REVIEW KEY VOCABULARY

- monomial
- degree of a monomial
- polynomial
- degree of a polynomial
- leading coefficient
- binomial
- trinomial
- roots
- vertical motion model
- perfect square trinomial
- factor by grouping
- factor completely

VOCABULARY EXERCISES

1. Copy and complete: The greatest degree of the terms in a polynomial is called the ? .
2. **WRITING** Is $2x^{-1}$ a monomial? *Explain* why or why not.
3. **WRITING** What does it mean for a polynomial to be factored completely? Give an example of a polynomial that has been factored completely.

In Exercises 4–6, match the polynomial with its classification.

- | | | |
|--------------|-------------|------------------|
| 4. $5x - 22$ | 5. $-11x^3$ | 6. $x^2 + x + 1$ |
| A. Monomial | B. Binomial | C. Trinomial |

REVIEW EXAMPLES AND EXERCISES

Use the review examples and exercises below to check your understanding of the concepts you have learned in each lesson of this chapter.

8.1 Add and Subtract Polynomials

EXAMPLE

Find the difference $(3x^2 + 2) - (4x^2 - x - 9)$.

Use a vertical format.

$$\begin{array}{r}
 3x^2 \quad + 2 \\
 - (4x^2 - x - 9) \\
 \hline
 \end{array}
 \quad \longrightarrow \quad
 \begin{array}{r}
 3x^2 \quad + 2 \\
 + \quad -4x^2 + x + 9 \\
 \hline
 -x^2 + x + 11
 \end{array}$$

EXERCISES

Find the sum or difference.

- | | |
|---|---|
| 7. $(9x + 6x^3 - 8x^2) + (-5x^3 + 6x)$ | 8. $(7a^3 - 4a^2 - 2a + 1) + (a^3 - 1)$ |
| 9. $(11y^5 + 3y^2 - 4) + (y^2 - y + 1)$ | 10. $(3n^2 - 4n + 1) - (8n^2 - 4n + 17)$ |
| 11. $(2s^3 + 8) - (-3s^3 + 7s - 5)$ | 12. $(-k^2 + 7k + 5) - (2k^4 - 3k^3 - 6)$ |

EXAMPLES 3 and 4
for Exs. 7–12

8.2 Multiply Polynomials

EXAMPLE

Find the product.

a. $(x^2 + 4x - 5)(2x - 1)$

b. $(5y + 6)(y - 3)$

Solution

a. Use a horizontal format.

$$(x^2 + 4x - 5)(2x - 1)$$

$$= x^2(2x - 1) + 4x(2x - 1) - 5(2x - 1) \quad \text{Write product.}$$

$$= 2x^3 - x^2 + 8x^2 - 4x - 10x + 5 \quad \text{Distributive property}$$

$$= 2x^3 + 7x^2 - 14x + 5 \quad \text{Combine like terms.}$$

b. Use a vertical format.

STEP 1 Multiply by -3 .

$$\begin{array}{r} 5y + 6 \\ \times \quad y - 3 \\ \hline -15y - 18 \end{array}$$

STEP 2 Multiply by y .

$$\begin{array}{r} 5y + 6 \\ \times \quad y - 3 \\ \hline -15y - 18 \\ 5y^2 + 6y \end{array}$$

STEP 3 Add products.

$$\begin{array}{r} 5y + 6 \\ \times \quad y - 3 \\ \hline -15y - 18 \\ 5y^2 + 6y \\ \hline 5y^2 - 9y - 18 \end{array}$$

EXERCISES

Find the product.

13. $(x^2 - 2x + 1)(x - 3)$

14. $(y^2 + 5y + 4)(3y + 2)$

15. $(x - 4)(x + 2)$

16. $(5b^2 - b - 7)(b + 6)$

17. $(z + 8)(z - 11)$

18. $(2a - 1)(a - 3)$

19. $(6n + 7)(3n + 1)$

20. $(4n - 5)(7n - 3)$

21. $(3x - 2)(x + 4)$

EXAMPLES
1, 2, 3, and 4
for Exs. 13–21

8.3 Find Special Products of Polynomials

EXAMPLE

Find the product $(3x + 2)(3x - 2)$.

$$(3x + 2)(3x - 2) = (3x)^2 - 2^2 \quad \text{Sum and difference pattern}$$

$$= 9x^2 - 4 \quad \text{Simplify.}$$

EXERCISES

Find the product.

22. $(x + 11)^2$

23. $(6y + 1)^2$

24. $(2x - y)^2$

25. $(4a - 3)^2$

26. $(k + 7)(k - 7)$

27. $(3s + 5)(3s - 5)$

EXAMPLES
1 and 2
for Exs. 22–27

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8.4 Solve Polynomial Equations in Factored Form

EXAMPLE

Solve $6x^2 + 42x = 0$.

$$6x^2 + 42x = 0 \quad \text{Write original equation.}$$

$$6x(x + 7) = 0 \quad \text{Factor left side.}$$

$$6x = 0 \quad \text{or} \quad x + 7 = 0 \quad \text{Zero-product property}$$

$$x = 0 \quad \text{or} \quad x = -7 \quad \text{Solve for } x.$$

▶ The solutions of the equation are 0 and -7 .

EXERCISES

Solve the equation.

28. $2a^2 + 26a = 0$

29. $3t^2 - 33t = 0$

30. $8x^2 - 4x = 0$

31. $m^2 = 9m$

32. $5y^2 = -50y$

33. $21h^2 = 7h$

EXAMPLES

3 and 4

for Exs. 28–33

8.5 Factor $x^2 + bx + c$

EXAMPLE

Factor $x^2 + 2x - 63$.

Find two factors of -63 whose sum is 2. One factor will be positive, and the other will be negative. Make an organized list of factors.

Factors of -63	Sum of factors	
1, -63	$1 + (-63) = -62$	✗
-1 , 63	$-1 + 63 = 62$	✗
3, -21	$3 + (-21) = -18$	✗
-3 , 21	$-3 + 21 = 18$	✗
9, -7	$9 + (-7) = 2$	← Correct sum
-9 , 7	$-9 + 7 = -2$	✗

▶ $x^2 + 2x - 63 = (x + 9)(x - 7)$

EXERCISES

Factor the trinomial.

34. $n^2 + 15n + 26$

35. $s^2 + 10s - 11$

36. $b^2 - 5b - 14$

37. $a^2 + 5a - 84$

38. $t^2 - 24t + 135$

39. $x^2 + 4x - 32$

40. $p^2 + 9p + 14$

41. $c^2 + 8c + 15$

42. $y^2 - 10y + 21$

EXAMPLES

1, 2 and 3

for Exs. 34–42

8.6 Factor $ax^2 + bx + c$

EXAMPLE

THROWN BALL You throw a ball up into the air. At 4 feet above the ground, the ball leaves your hand with an initial vertical velocity of 30 feet per second.

- Write an equation that gives the height (in feet) of the ball as a function of the time (in seconds) since it left your hand.
- After how many seconds does the ball land on the ground?

Solution

- Use the vertical motion model $h = -16t^2 + vt + s$ to write an equation for the height h (in feet) of the ball as a function of the time t (in seconds). In this case, $v = 30$ and $s = 4$.

$$h = -16t^2 + vt + s \quad \text{Vertical motion model}$$

$$h = -16t^2 + 30t + 4 \quad \text{Substitute 30 for } v \text{ and 4 for } s.$$

- When the ball lands on the ground, its height is 0 feet. Substitute 0 for h and solve the equation for t .

$$0 = -16t^2 + 30t + 4 \quad \text{Substitute 0 for } h.$$

$$0 = -2(8t^2 - 15t - 2) \quad \text{Factor out } -2.$$

$$0 = -2(8t + 1)(t - 2) \quad \text{Factor the trinomial. Find factors of 8 and } -2 \text{ that produce a middle term with a coefficient of } -15.$$

$$8t + 1 = 0 \quad \text{or} \quad t - 2 = 0 \quad \text{Zero-product property}$$

$$t = -\frac{1}{8} \quad \text{or} \quad t = 2 \quad \text{Solve for } t.$$

The solutions of the equation are $-\frac{1}{8}$ and 2. A negative solution does not make sense in this situation, so disregard $-\frac{1}{8}$.

► The ball lands on the ground after 2 seconds.

EXERCISES

Solve the equation.

43. $7x^2 - 8x = -1$

44. $4n^2 + 3 = 7n$

45. $3s^2 + 4s + 4 = 8$

46. $6z^2 + 13z = 5$

47. $-4r^2 = 18r + 18$

48. $9a^2 = 6a + 24$

49. **THROWN BALL** You throw a ball up into the air with an initial vertical velocity of 46 feet per second. The ball leaves your hand when it is 6 feet above the ground. After how many seconds does the ball land on the ground?

50.  **GEOMETRY** The length of a rectangle is 1 inch less than twice the width. The area of the rectangle is 21 square inches. What is the length of the rectangle?

EXAMPLES
1, 2, 3, and 4
for Exs. 43–50

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8.7 Factor Special Products

EXAMPLE

Factor the polynomial.

a. $100x^2 - y^2$

b. $4x^2 - 36x + 81$

Solution

$$\begin{aligned} \text{a. } 100x^2 - y^2 &= (10x)^2 - y^2 \\ &= (10x + y)(10x - y) \end{aligned}$$

Write as $a^2 - b^2$.

Difference of two squares pattern

$$\begin{aligned} \text{b. } 4x^2 - 36x + 81 &= (2x)^2 - 2(2x \cdot 9) + 9^2 \\ &= (2x - 9)^2 \end{aligned}$$

Write as $a^2 - 2ab + b^2$.

Perfect square trinomial pattern

EXERCISES

Factor the polynomial.

51. $z^2 - 225$

52. $a^2 - 16y^2$

53. $12 - 48n^2$

54. $x^2 + 20x + 100$

55. $16p^2 - 8p + 1$

56. $-2y^2 + 32y - 128$

57. **DROPPED OBJECT** You drop a penny from a height of 16 feet. After how many seconds does the penny land on the ground?

EXAMPLES
1, 2, 3, 4, and 6
for Exs. 51–57

8.8 Factor Polynomials Completely

EXAMPLE

Factor the polynomial completely.

a. $y^3 - 4y^2 + 8y - 32$

b. $5x^3 - 40x^2 + 80x$

Solution

$$\begin{aligned} \text{a. } y^3 - 4y^2 + 8y - 32 &= (y^3 - 4y^2) + (8y - 32) \\ &= y^2(y - 4) + 8(y - 4) \\ &= (y - 4)(y^2 + 8) \end{aligned}$$

Group terms.

Factor each group.

Distributive property

$$\begin{aligned} \text{b. } 5x^3 - 40x^2 + 80x &= 5x(x^2 - 8x + 16) \\ &= 5x(x - 4)^2 \end{aligned}$$

Factor out 5x.

Perfect square trinomial pattern

EXERCISES

Factor the polynomial completely.

58. $a^3 + 6a - 5a^2 - 30$

59. $y^2 + 3y + yx + 3x$

60. $x^3 - 11x^2 - x + 11$

61. $5s^4 - 125s^2$

62. $147n^5 - 3n^3$

63. $2z^3 + 2z^2 - 60z$

64. $x^3 + 5x^2 - x - 5$

65. $2b^3 + 3b^2 - 8b - 12$

66. $x^3 + x^2 - 6x - 6$

EXAMPLE 4
for Exs. 58–66