

LESSON
8.3**Study Guide**

For use with the lesson "Find Special Products of Polynomials"

GOAL Use special product patterns to multiply polynomials.**Square of a Binomial Pattern****Algebra**

$$(a + b)^2 = a^2 + 2ab + b^2$$

$$(a - b)^2 = a^2 - 2ab + b^2$$

Example

$$(x + 3)^2 = x^2 + 6x + 9$$

$$(3x - 2)^2 = 9x^2 - 12x + 4$$

EXAMPLE 1**Use the square of a binomial pattern****Find the product.**

a. $(7x + 2)^2$

b. $(6x - 5y)^2$

Solution

a.
$$(7x + 2)^2 = (7x)^2 + 2(7x)(2) + 2^2$$
$$= 49x^2 + 28x + 4$$

Square of a binomial pattern
Simplify.

b.
$$(6x - 5y)^2 = (6x)^2 - 2(6x)(5y) + (5y)^2$$
$$= 36x^2 - 60xy + 25y^2$$

Square of a binomial pattern
Simplify.**Exercises for Example 1****Find the product.**

1. $(y + 9)^2$

2. $(3z + 7)^2$

3. $(2w - 3)^2$

4. $(10r - 3s)^2$

Sum and Difference Pattern**Algebra**

$$(a + b)(a - b) = a^2 - b^2$$

Example

$$(x + 5)(x - 5) = x^2 - 25$$

LESSON
8.3**Study Guide** *continued*
*For use with the lesson "Find Special Products of Polynomials"***EXAMPLE 2** **Use the sum and difference pattern****Find the product.**

a. $(m + 9)(m - 9)$

b. $(4n - 3)(4n + 3)$

Solution

$$\begin{aligned} \text{a. } (m + 9)(m - 9) &= m^2 - 9^2 && \text{Sum and difference pattern} \\ &= m^2 - 81 && \text{Simplify.} \end{aligned}$$

$$\begin{aligned} \text{b. } (4n - 3)(4n + 3) &= (4n)^2 - 3^2 && \text{Sum and difference pattern} \\ &= 16n^2 - 9 && \text{Simplify.} \end{aligned}$$

Exercises for Example 2**Find the product.**

5. $(g + 11)(g - 11)$

6. $(7f - 1)(7f + 1)$

7. $(2h + 9)(2h - 9)$

8. $(6k - 8)(6k + 8)$

EXAMPLE 3 **Use special products and mental math****Use special products to find the product of $37 \cdot 43$.****Solution**

Notice that 37 is 3 less than 40 while 43 is 3 more than 40.

$$\begin{aligned} 37 \cdot 43 &= (40 - 3)(40 + 3) && \text{Write as a product of difference and sum.} \\ &= 40^2 - 3^2 && \text{Sum and difference pattern} \\ &= 1600 - 9 && \text{Evaluate powers.} \\ &= 1591 && \text{Simplify.} \end{aligned}$$

Exercises for Example 3**Describe how you can use special products to find the product.**

9. 55^2

10. $31 \cdot 49$