

# Study Guide and Intervention

## Factoring Differences of Squares

**Factor  $a^2 - b^2$**  The binomial expression  $a^2 - b^2$  is called the **difference of two squares**. The following pattern shows how to factor the difference of squares.

Difference of Squares	$a^2 - b^2 = (a - b)(a + b) = (a + b)(a - b)$ .
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**Example 1** Factor each binomial.

a.  $n^2 - 64$

$$\begin{aligned} n^2 - 64 &= n^2 - 8^2 && \text{Write in the form } a^2 - b^2. \\ &= (n + 8)(n - 8) && \text{Factor.} \end{aligned}$$

b.  $4m^2 - 81n^2$

$$\begin{aligned} 4m^2 - 81n^2 &= (2m)^2 - (9n)^2 && \text{Write in the form } a^2 - b^2. \\ &= (2m - 9n)(2m + 9n) && \text{Factor.} \end{aligned}$$

**Example 2** Factor each polynomial.

a.  $50a^2 - 72$

$$\begin{aligned} 50a^2 - 72 &= 2(25a^2 - 36) && \text{Find the GCF.} \\ &= 2[(5a)^2 - 6^2] && 25a^2 = 5a \cdot 5a \text{ and } 36 = 6 \cdot 6 \\ &= 2(5a + 6)(5a - 6) && \text{Factor the difference of squares.} \end{aligned}$$

b.  $4x^4 + 8x^3 - 4x^2 - 8x$

$$\begin{aligned} 4x^4 + 8x^3 - 4x^2 - 8x & \text{Original polynomial} \\ &= 4x(x^3 + 2x^2 - x - 2) && \text{Find the GCF.} \\ &= 4x[(x^3 + 2x^2) - (x + 2)] && \text{Group terms.} \\ &= 4x[x^2(x + 2) - 1(x + 2)] && \text{Find the GCF.} \\ &= 4x[(x^2 - 1)(x + 2)] && \text{Factor by grouping.} \\ &= 4x[(x - 1)(x + 1)(x + 2)] && \text{Factor the difference of squares.} \end{aligned}$$

### Exercises

Factor each polynomial if possible. If the polynomial cannot be factored, write *prime*.

1.  $x^2 - 81$

2.  $m^2 - 100$

3.  $16n^2 - 25$

4.  $36x^2 - 100y^2$

5.  $49x^2 - 32$

6.  $16a^2 - 9b^2$

7.  $225c^2 - a^2$

8.  $72p^2 - 50$

9.  $-2 + 2x^2$

10.  $-81 + a^4$

11.  $6 - 54a^2$

12.  $8y^2 - 200$

13.  $4x^3 - 100x$

14.  $2y^4 - 32y^2$

15.  $8m^3 - 128m$

16.  $6x^2 - 25$

17.  $2a^3 - 98ab^2$

18.  $18y^2 - 72y^4$

19.  $169x^3 - x$

20.  $3a^4 - 3a^2$

21.  $3x^4 + 6x^3 - 3x^2 - 6x$

## Study Guide and Intervention *(continued)*

### Factoring Differences of Squares

**Solve Equations by Factoring** Factoring and the Zero Product Property can be used to solve equations that can be written as the product of any number of factors set equal to 0.

#### Example

Solve each equation. Check your solutions.

a.  $x^2 - \frac{1}{25} = 0$

$$x^2 - \frac{1}{25} = 0 \quad \text{Original equation}$$

$$x^2 - \left(\frac{1}{5}\right)^2 = 0 \quad x^2 = x \cdot x \text{ and } \frac{1}{25} = \left(\frac{1}{5}\right)\left(\frac{1}{5}\right)$$

$$\left(x + \frac{1}{5}\right)\left(x - \frac{1}{5}\right) = 0 \quad \text{Factor the difference of squares.}$$

$$x + \frac{1}{5} = 0 \quad \text{or} \quad x - \frac{1}{5} = 0 \quad \text{Zero Product Property}$$

$$x = -\frac{1}{5} \quad x = \frac{1}{5} \quad \text{Solve each equation.}$$

The solution set is  $\left\{-\frac{1}{5}, \frac{1}{5}\right\}$ . Since  $\left(-\frac{1}{5}\right)^2 - \frac{1}{25} = 0$  and  $\left(\frac{1}{5}\right)^2 - \frac{1}{25} = 0$ , the solutions check.

b.  $4x^3 = 9x$

$$4x^3 = 9x \quad \text{Original equation}$$

$$4x^3 - 9x = 0 \quad \text{Subtract } 9x \text{ from each side.}$$

$$x(4x^2 - 9) = 0 \quad \text{Find the GCF.}$$

$$x[(2x)^2 - 3^2] = 0 \quad 4x^2 = 2x \cdot 2x \text{ and } 9 = 3 \cdot 3$$

$$x[(2x)^2 - 3^2] = x[(2x - 3)(2x + 3)] \quad \text{Factor the difference of squares.}$$

$$x = 0 \quad \text{or} \quad (2x - 3) = 0 \quad \text{or} \quad (2x + 3) = 0 \quad \text{Zero Product Property}$$

$$x = 0 \quad x = \frac{3}{2} \quad x = -\frac{3}{2} \quad \text{Solve each equation.}$$

The solution set is  $\left\{0, \frac{3}{2}, -\frac{3}{2}\right\}$ .

Since  $4(0)^3 = 9(0)$ ,  $4\left(\frac{3}{2}\right)^3 = 9\left(\frac{3}{2}\right)$ , and  $4\left(-\frac{3}{2}\right)^3 = 9\left(-\frac{3}{2}\right)$ , the solutions check.

#### Exercises

Solve each equation. Check your solutions.

1.  $81x^2 = 49$

2.  $36n^2 = 1$

3.  $25d^2 - 100 = 0$

4.  $\frac{1}{4}x^2 = 25$

5.  $36 = \frac{1}{25}x^2$

6.  $\frac{49}{100} - x^2 = 0$

7.  $9x^3 = 25x$

8.  $7a^3 = 175a$

9.  $2m^3 = 32m$

10.  $16y^3 = 25y$

11.  $\frac{1}{64}x^2 = 49$

12.  $4a^3 - 64a = 0$

13.  $3b^3 - 27b = 0$

14.  $\frac{9}{25}m^2 = 121$

15.  $48n^3 = 147n$



